

# Modelling Gyrosynchrotron Emission from Energetic Electrons in CME Flux Ropes

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# Outline

- Introduction
- Modelling Framework
- Simulation Results
- Summary and Outlook

# Introduction

# Type IV Radio Bursts

- The solar atmosphere is a rich source of radio emission, especially during/after solar flares and CMEs
- Type IV bursts: broadband continua, often containing bursty features, during/after CMEs and flares
- Complex interplay of processes
  - **Coherent vs. incoherent** emission (Melrose 2017)
  - **Spontaneous vs. stimulated** emission (Papadopoulos & Freund 1979)
  - **Thermal vs. nonthermal** processes (Pick & Vilmer 2008)

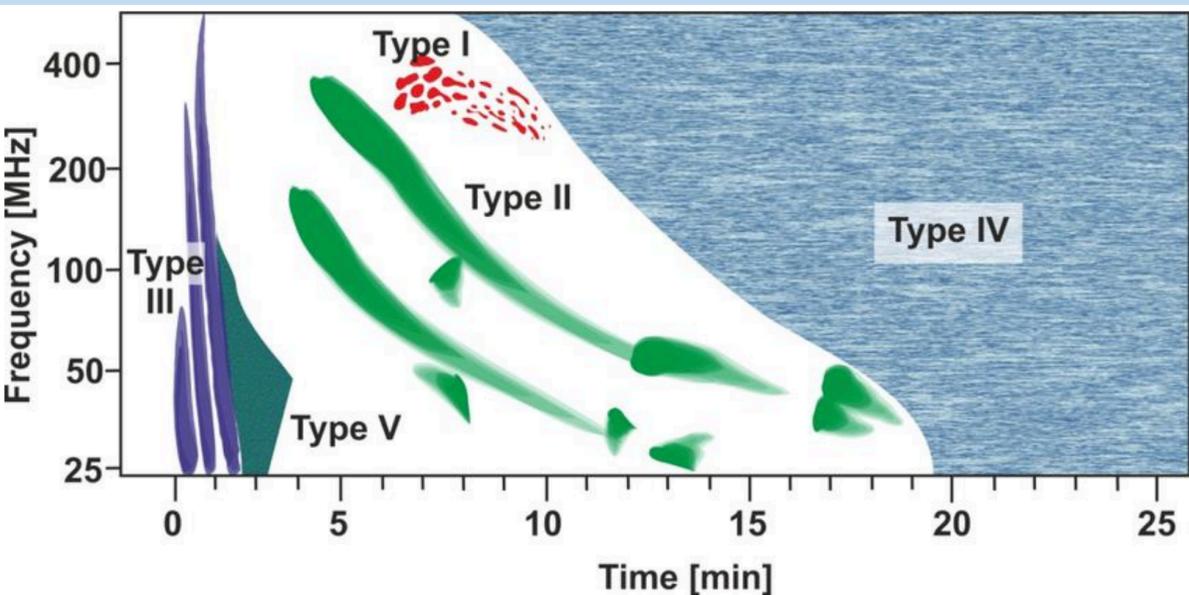


Fig: Different types of radio bursts (Shamsuddin+2023)

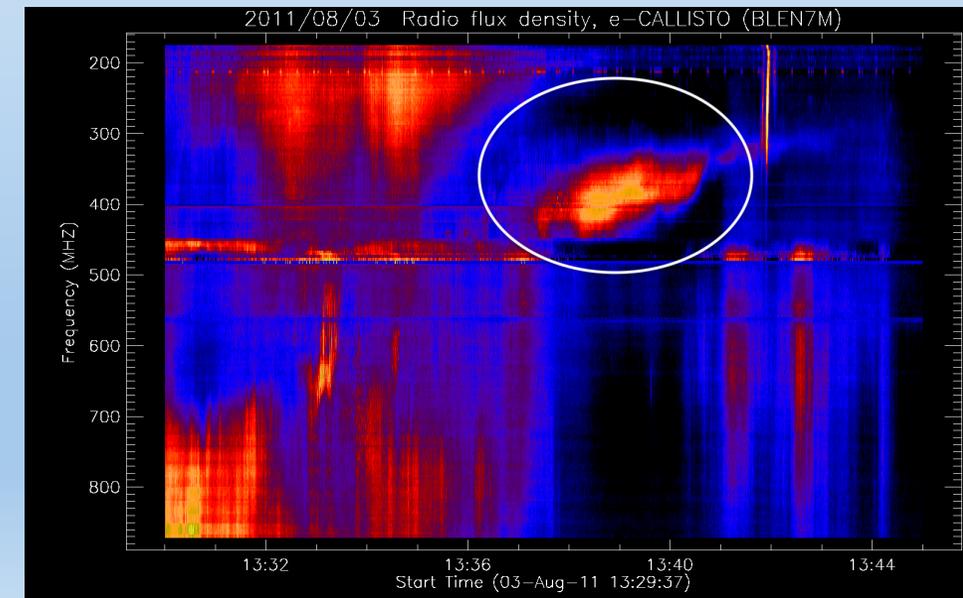
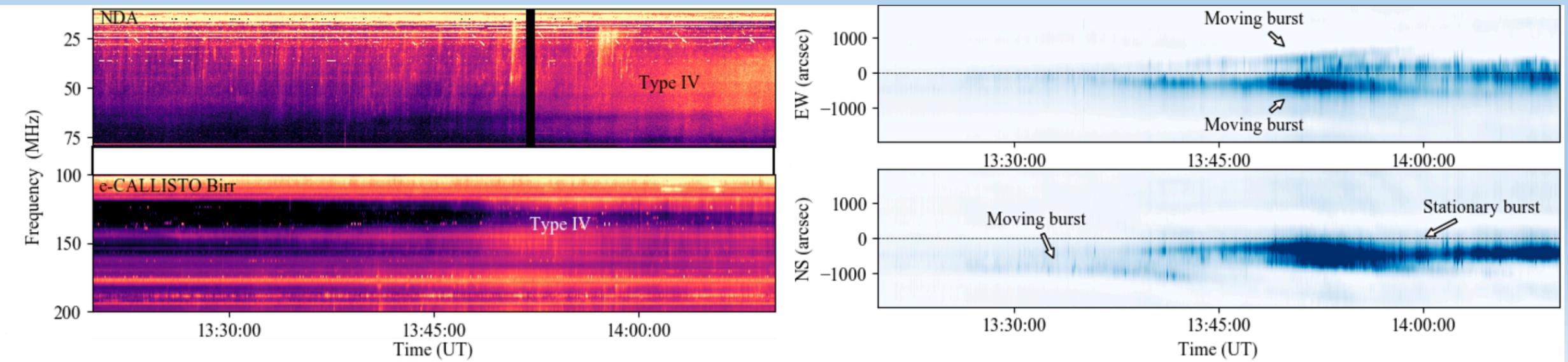


Fig: Dynamic radio spectrum of a type IV burst

# Challenges in Interpreting Type IV Bursts

- Disentangling emission mechanisms (Morosan+2019)
- **Diagnosing** CME magnetic fields from radio spectra (Mondal+2020)
- **Stationary** (IVs) vs. **moving** (IVm) type IV sources (Morosan+2021)
  - Spectral drift  $\neq$  spatial drift – imaging reveals spatial motion **even without** frequency drift
- IVm/IVs classification is blurred
  - Gyrosynchrotron (GS) sources naturally show spatial drift (CME motion); apparent stationarity can result from coherent emission processes

Morosan+2021



# Aims and Coupled Modelling Approach

## Aims:

- Simulate **GS emission** from energetic electrons trapped in erupting CME flux ropes
- Move **beyond idealised assumptions** about corona and electron distributions
- Investigate **how synthetic type IV spectra are shaped** by:
  - Variations in the electron energy distributions
  - CME properties and dynamics
  - Observer perspective

# Aims and Coupled Modelling Approach

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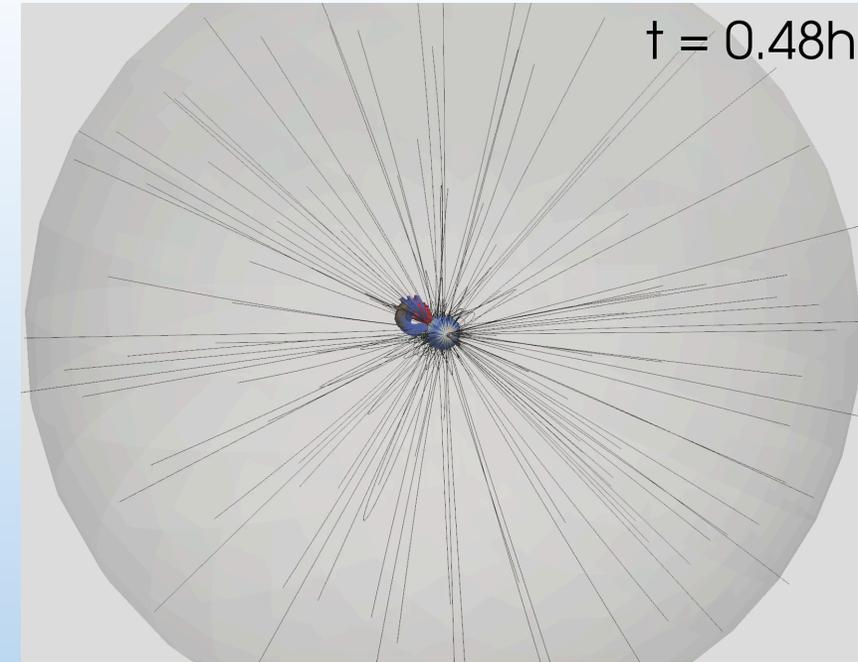
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  - Observer perspective

## Coupled Modelling Approach:

- Modular simulation chain linking:
  - **Coronal plasma dynamics** including CMEs (MHD model)
  - **Energetic electron transport** (particle transport code)
  - **Radio emission synthesis** (gyrosynchrotron code)

# Modelling Framework

# Modelling Framework



Husidic+2024

## COCONUT - COolfluid COroNal Unstructured

- 3D **ideal MHD** model of the corona (Perri+2023)
- CME: unstable Titov-Démoulin **flux rope** (Linan+2023)

## PARADISE (PARTicle Radiation Asset Directed at Interplanetary Space Exploration)

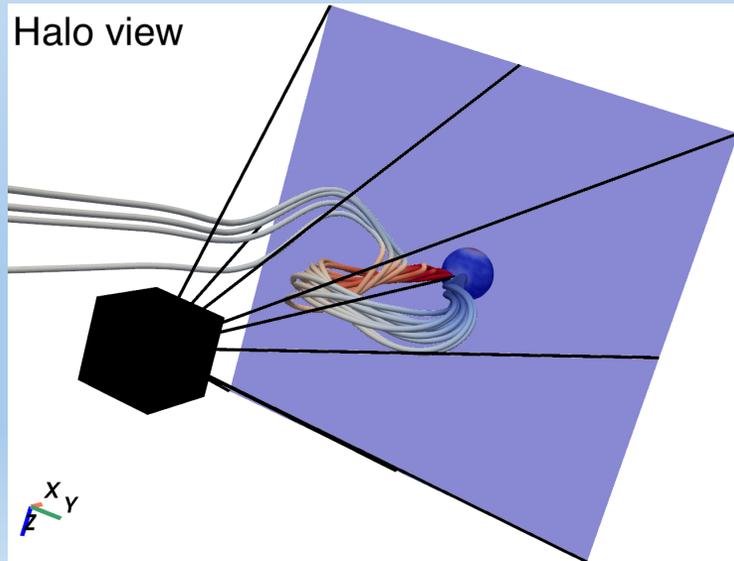
- Evolves energetic particles through dynamic MHD fields
- Solves **focused transport equation** stochastically (Wijsen 2020)

## Ultimate Fast Gyrosynchrotron Codes (UFGSCs)

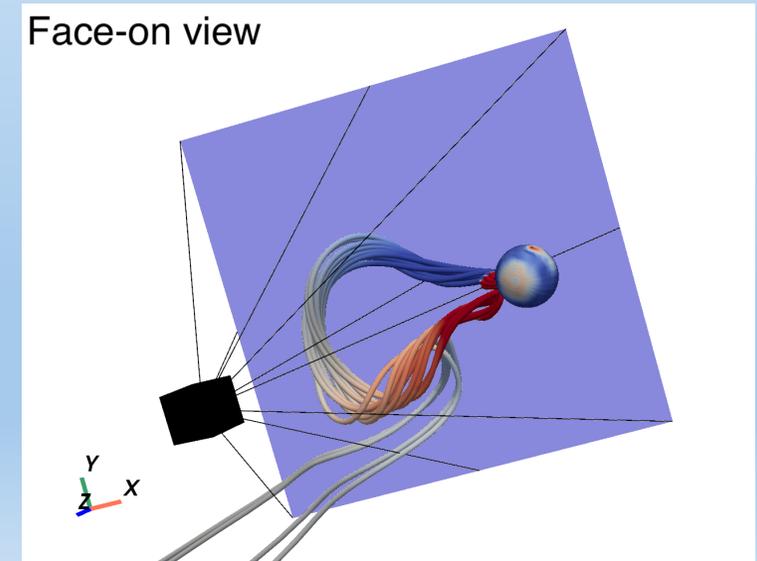
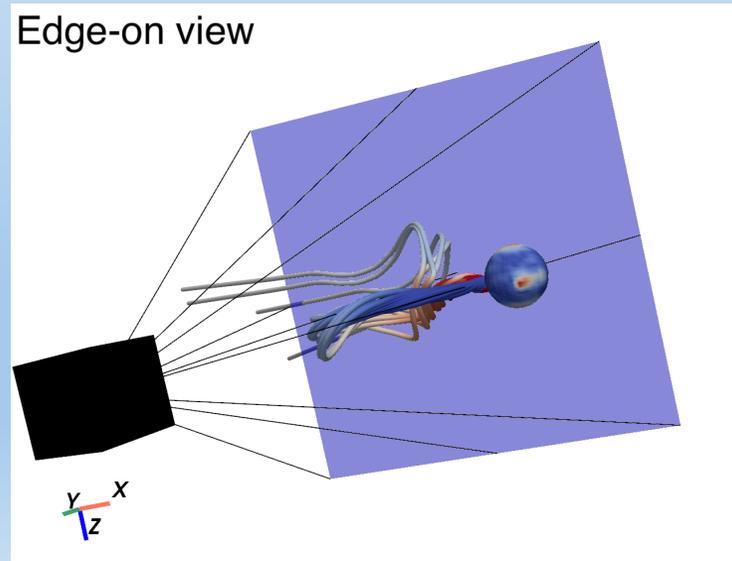
- Calculate **GS emission** and **absorption**
- Use **fast, accurate numerical approximations** (Fleishman & Kuznetsov 2010)
- Allow for **arbitrary electron distributions** (Kuznetsov & Fleishman 2021)

# Simulation Setup

- **Two eruption strengths** in the CME simulation:
  - $\zeta = 30 \rightarrow B_0 \approx 5.8 \text{ G}; v_0 \approx 940 \text{ km/s}$
  - $\zeta = 70 \rightarrow B_0 \approx 10.6 \text{ G}; v_0 \approx 1300 \text{ km/s}$
- **Two power-law indices** for electron injections:  $\delta = 2$  and  $\delta = 3$  (10 keV to 10 MeV)
- **Three observer perspectives** (“**halo view**”, “**edge-on view**”, “**face-on view**”) with defined **viewing fields**
- **Calculate GS emission along lines of sight** and integrate over observer’s field of view



Observer is inside the corona ( $r < 0.1 \text{ au} = 21.5 \text{ solar radii}$ )



Husidic et al. (submitted)

# Simulation Results

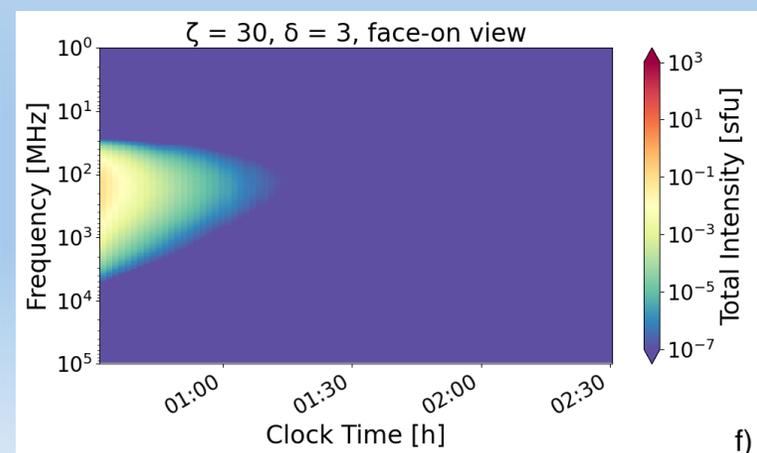
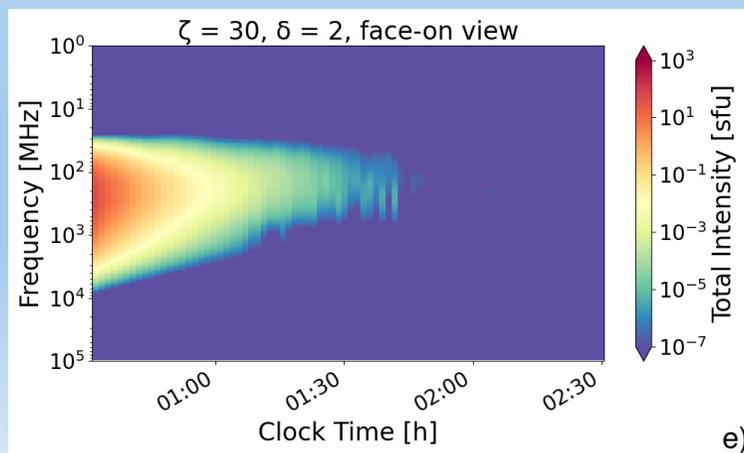
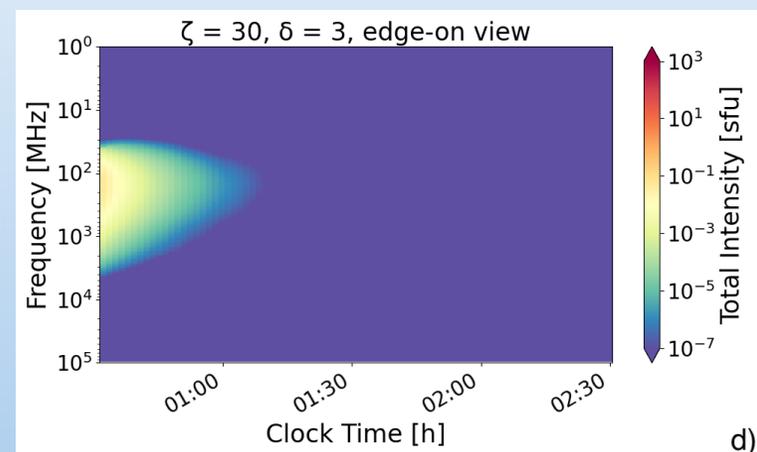
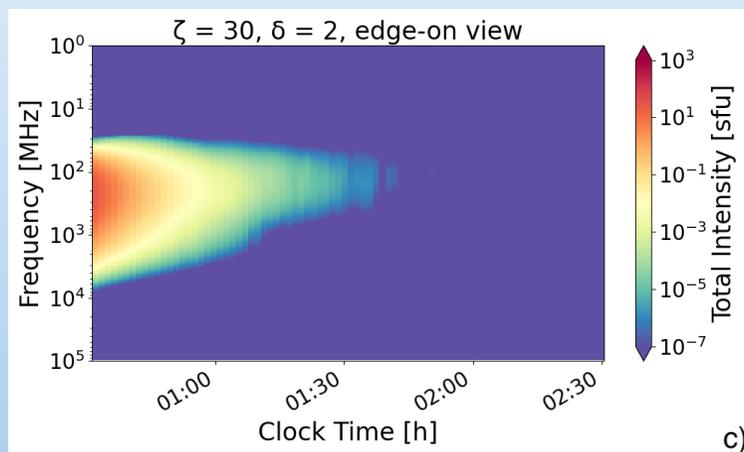
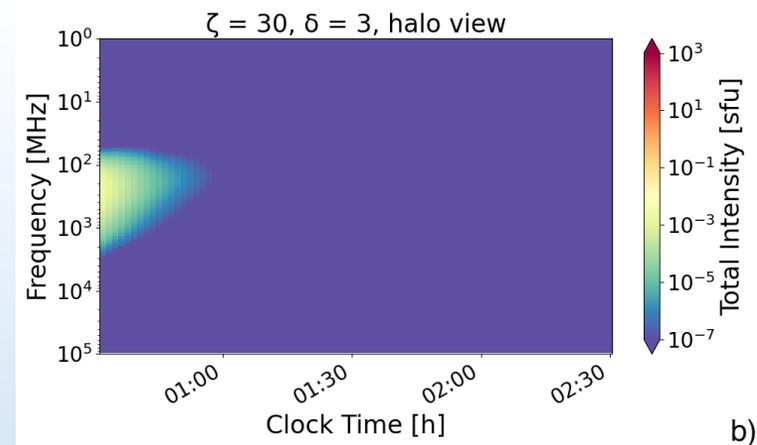
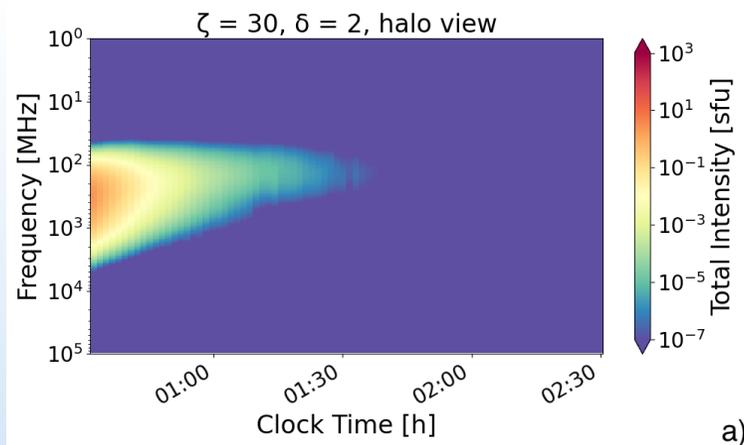
# CME Case $\zeta = 30$

Peak intensity ratios across  $\delta$ -values:

View	$I_{\delta=2}/I_{\delta=3}$
halo	1100
edge-on	564
face-on	560

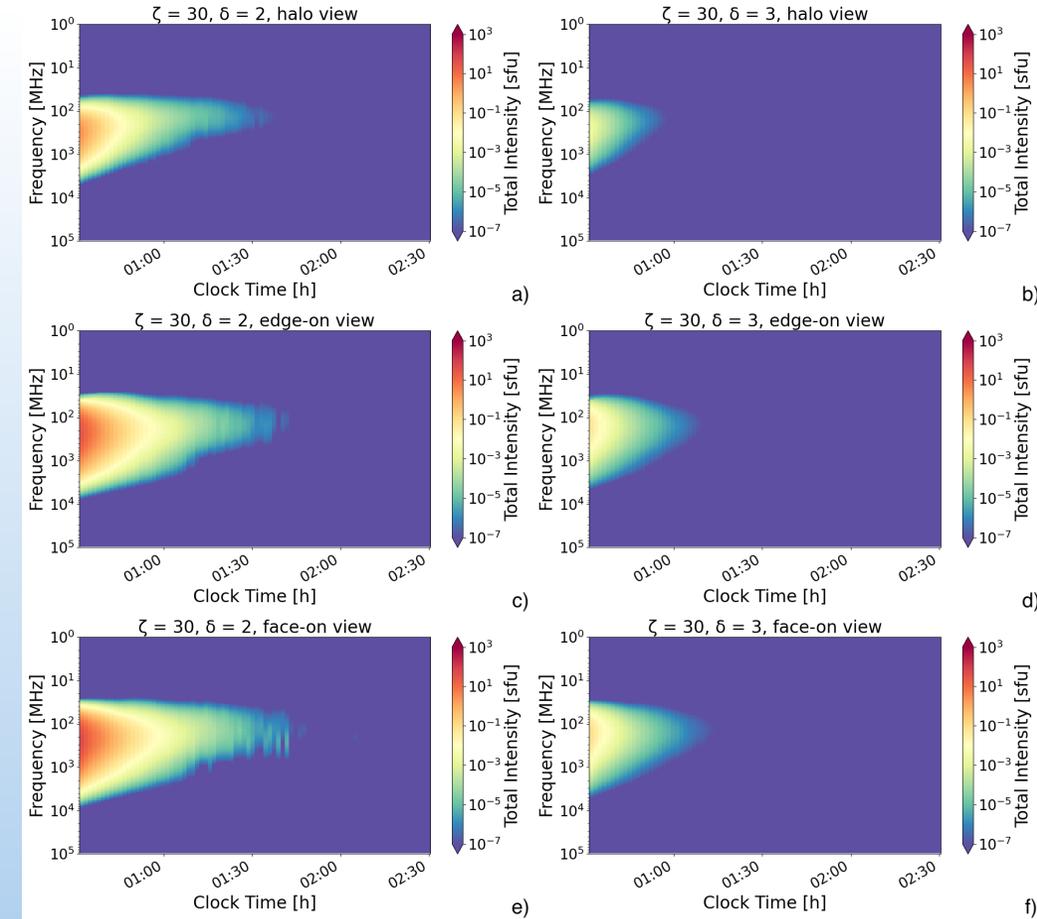
Peak intensity ratios across views:

$\delta$	$I_{\text{edge-on}}/I_{\text{halo}}$	$I_{\text{face-on}}/I_{\text{halo}}$
2	13.1	22.5
3	25.5	44.1

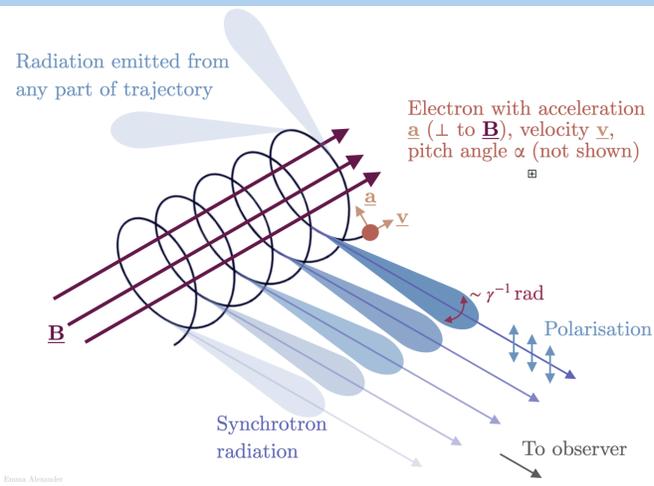


# CME Case $\zeta = 30$

- **Flatter spectrum ( $\delta = 2$ )**  $\rightarrow$  more high-energy electrons  $\rightarrow$  **stronger and longer lasting GS emission**
- **GS intensity depends on B-field strength and observer geometry**
  - **Helio view:** weakest emission (aligned fields, thinner region)
  - **Edge-on view:** stronger emission (thicker flux rope cross section, stronger fields)
  - **Face-on view:** strongest emission (optimal viewing angle + large region)



Husidic et al. (submitted)



Credit: Emma Alexander, under CC BY 4.0.

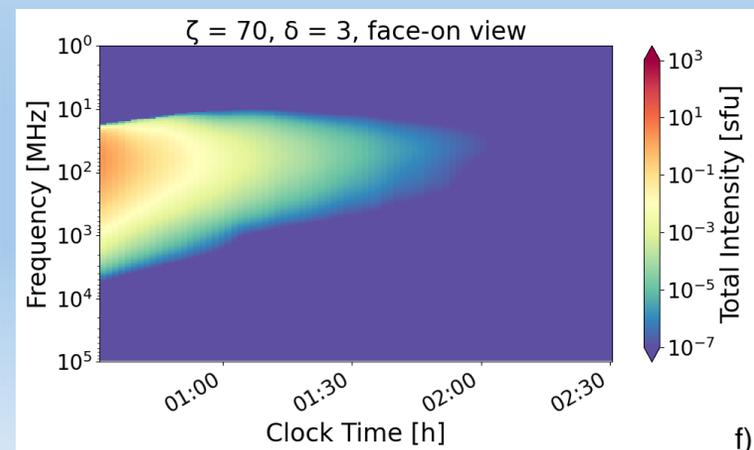
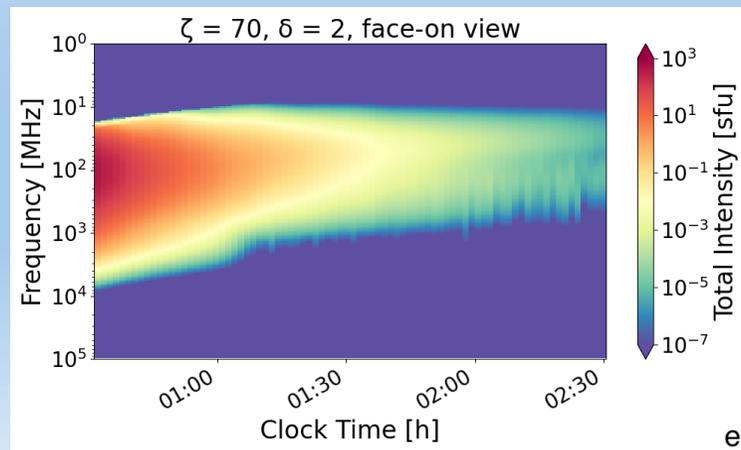
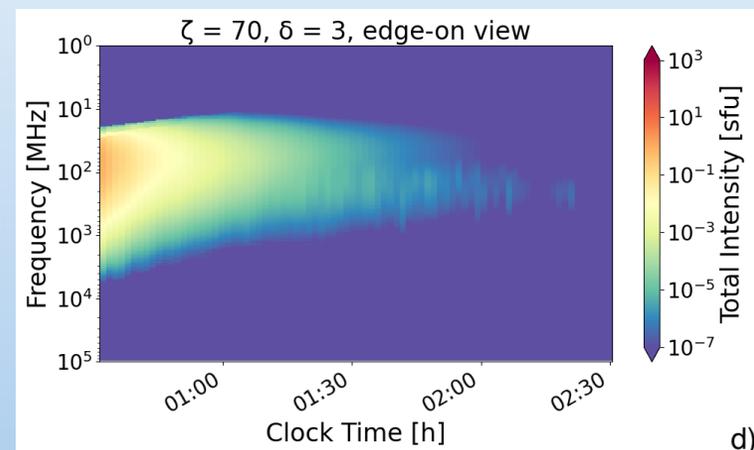
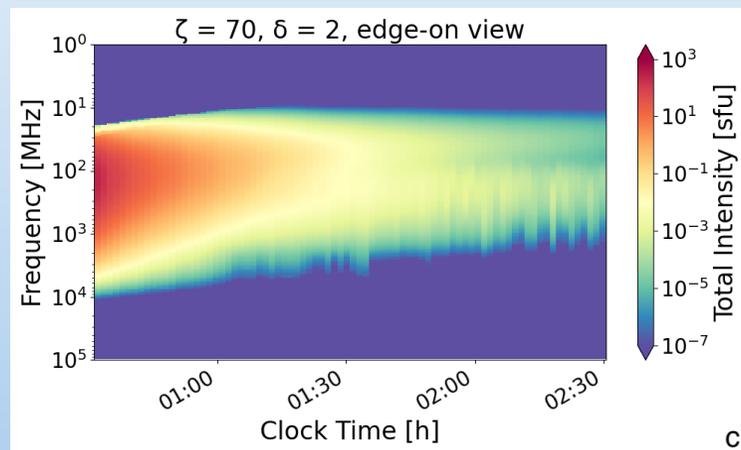
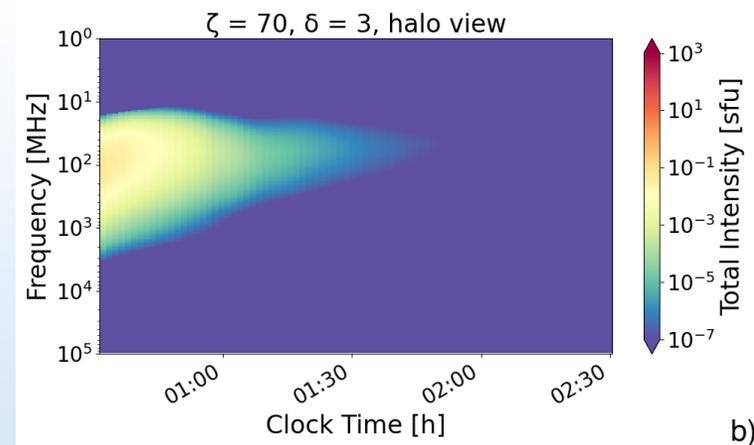
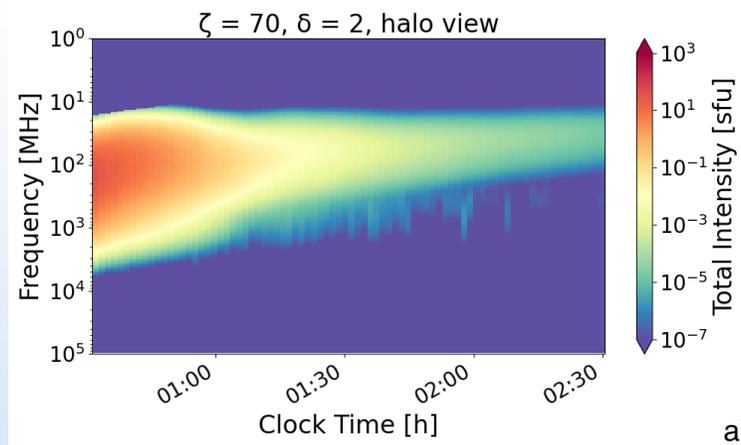
# CME Case $\zeta = 70$

Peak intensity ratios across  $\delta$ -values:

View	$I_{\delta=2}/I_{\delta=3}$
halo	620
edge-on	310
face-on	208

Peak intensity ratios across views:

$\delta$	$I_{\text{edge-on}}/I_{\text{halo}}$	$I_{\text{face-on}}/I_{\text{halo}}$
2	7.2	12.8
3	14.3	38.1

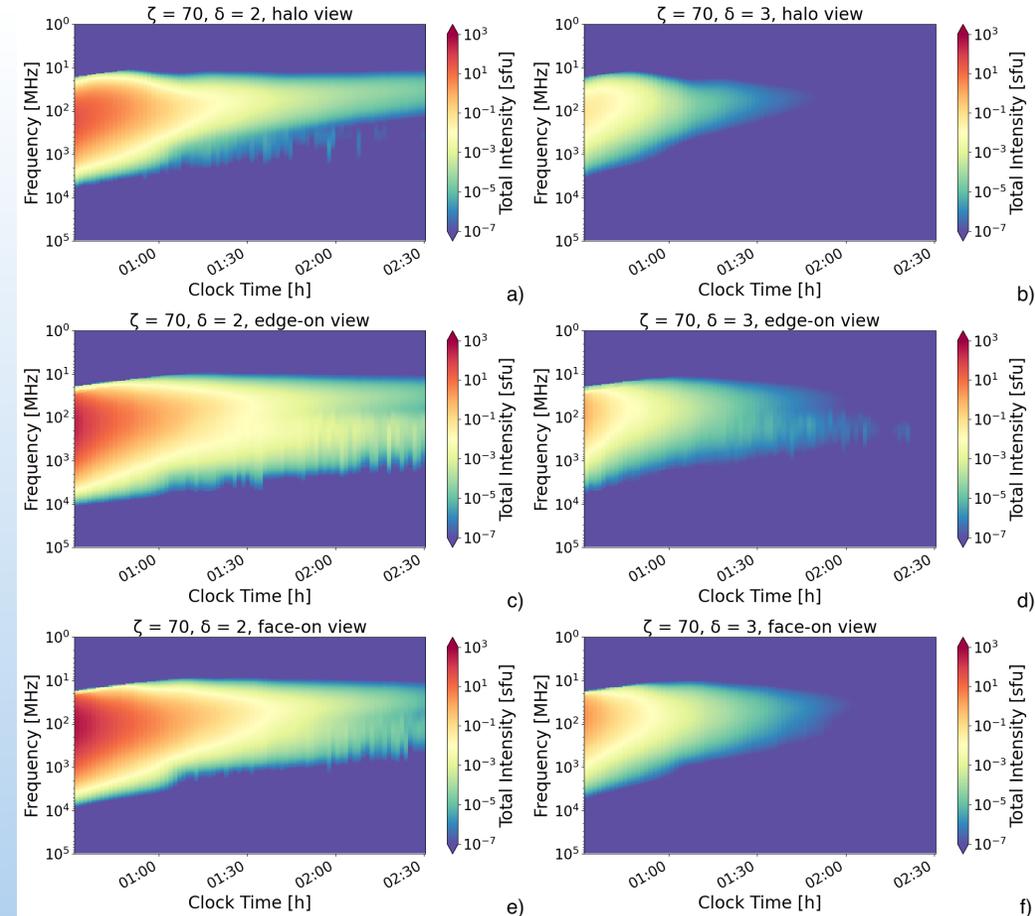


# CME Case $\zeta = 70$

- Similar trends as  $\zeta = 30$  cases
- Secondary emission lane detected at higher frequencies (edge-on/face-on views)
  - Localised GS enhancements from stronger B-fields

$$P_{\text{syn}} \approx \frac{4}{3} \sigma_{\text{T}} c \gamma^2 \beta^2 U_{\text{B}} \sin^2 \alpha$$

$\sigma_{\text{T}}$ : Thomson scattering cross-section  
 $\beta = v/c$   
 $U_{\text{B}} = B^2/(8\pi)$  magnetic energy density  
 $\alpha$ : pitch-angle



Husidic et al. (submitted)

# Intensity Ratios across CME Cases

## (3) Intensity ratios across CME cases

$\delta$	View	$I_{\zeta=70}/I_{\zeta=30}$
2	halo	16.2
	edge-on	8.9
	face-on	9.2
3	halo	28.6
	edge-on	16.1
	face-on	24.7

Husidic et al. (submitted)

$\zeta = 70$  CME yields stronger GS emission across vantage points

Stronger magnetic fields  $\rightarrow$  increased synchrotron power

Stronger field gradients enhance electron trapping and GS emission

$$P_{\text{syn}} \approx \frac{4}{3} \sigma_{\text{T}} c \gamma^2 \beta^2 U_{\text{B}} \sin^2 \alpha$$

$\sigma_{\text{T}}$ : Thomson scattering cross-section

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$U_{\text{B}} = B^2/(8\pi)$  magnetic energy density

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# Summary and Outlook

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- **Coupled Numerical Models**
  - **COCONUT** : 3D MHD coronal model
  - **PARADISE** : Energetic particle transport simulations
  - **UFGSCs** : Fast GS emission computations
- **Modelling GS Emission in the Corona**
  - Type IV spectra are shaped by **electron index**, **CME properties**, and **observer geometry**
  - Strongest GS emission originates from **CME legs**
  - Results support **GS** as a **key contributor** of type IV bursts
  - **Coherent** plasma processes **cannot be excluded**
- **Outlook**
  - Future parametric studies will explore how **CME B-fields** shape GS signatures
  - Aim to address the **stationary vs. moving type IV conundrum**
  - Use **PSP in situ data** (radio waves, particles) to **constrain model** and link to **observed events**

**Backup Slides**

# Peak Intensity Frequency Drift

- All obtained spectra exhibit similar structure, featuring a high-intensity centre surrounded by weaker emission, with the peak drifting towards lower frequencies over time
- Compare to characteristic synchrotron peak frequency (Ginzburg 1979)
- Both CME expansion and adiabatic cooling contribute to observed downward drift in the simulation results

$$\nu_{\text{peak}}(t) = \frac{3}{4\pi} \frac{e B(t)}{m_e c} \gamma^2 = \frac{3}{4\pi} \nu_g(t) \gamma^2$$

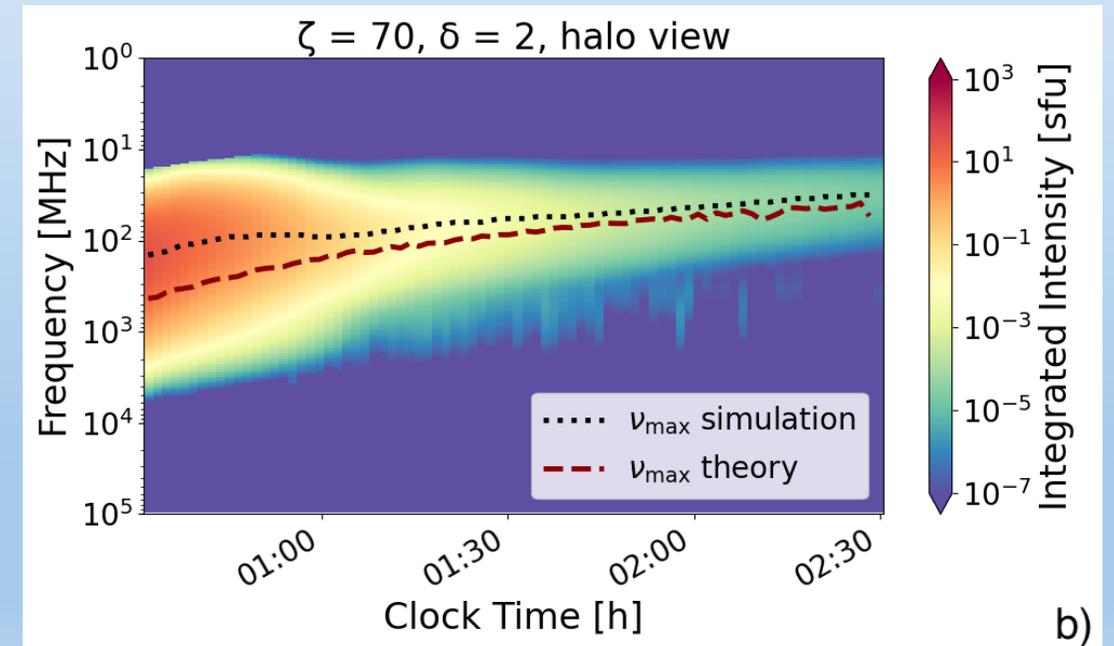
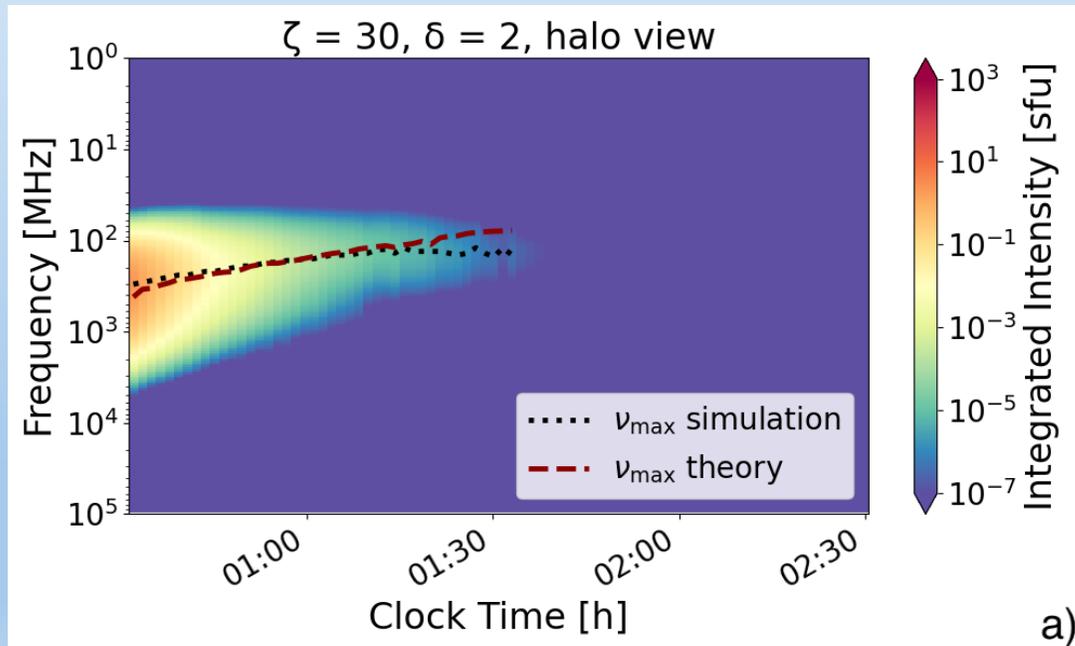
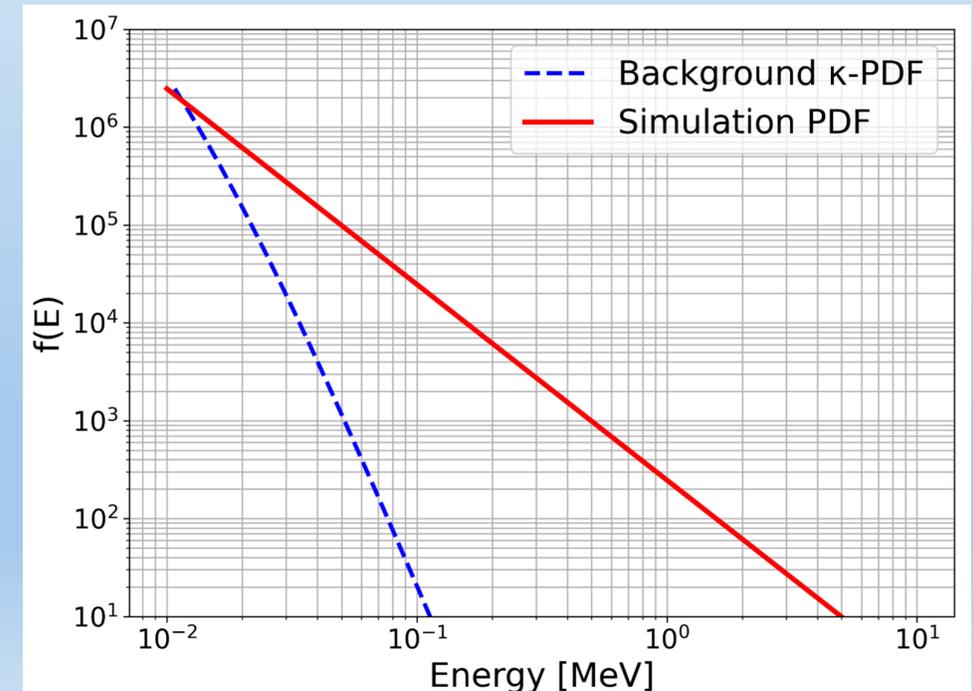


Fig: Peak intensity frequency drifts from simulation and theory (Husidic et al., submitted)

# PARADISE Distribution Scaling

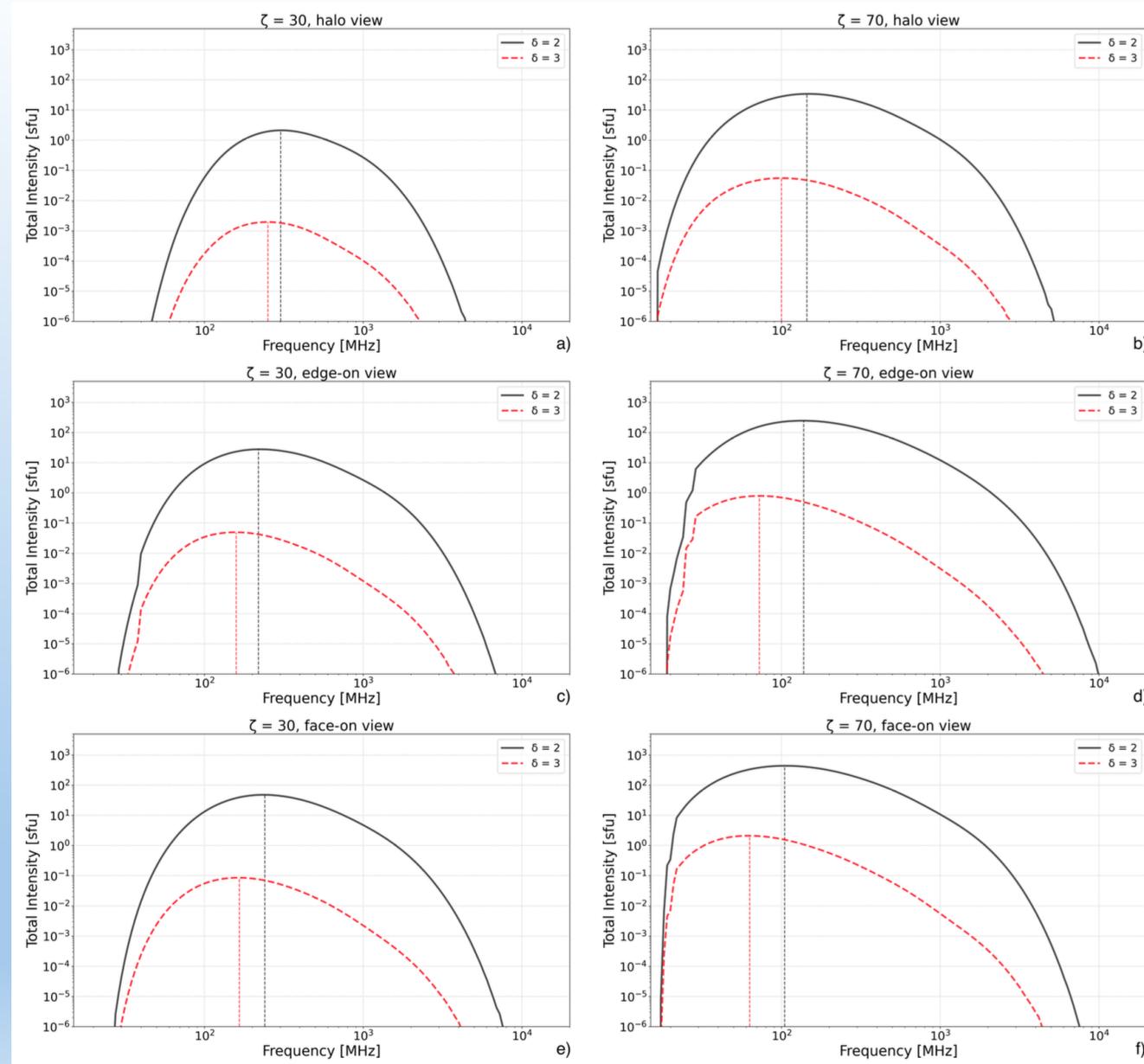
- Output: differential intensity  $j(\mathbf{x}, \mathbf{p}, t) = p^2 f(\mathbf{x}, \mathbf{p}, t)$
- Provide electron distributions as  $f_{i,j} = f(E_i, \mu_j)$  to the UFGSCs, where energies are logarithmically spaced
- PARADISE distribution scaled to match a (relativistic regularised) Kappa distribution (rRKD,  $\kappa = 8$ ) at 10 keV at injection location and injection time
- To avoid exact zeros in the electron distribution, an rRKD background is added
- Background ensures:
  - Physical units of  $f$
  - Avoiding excessively steep gradients in  $f$  that could otherwise provide conditions for maser instability to grow
- Background contribution to GS emission is negligible (< 0.01 % at peak intensity)



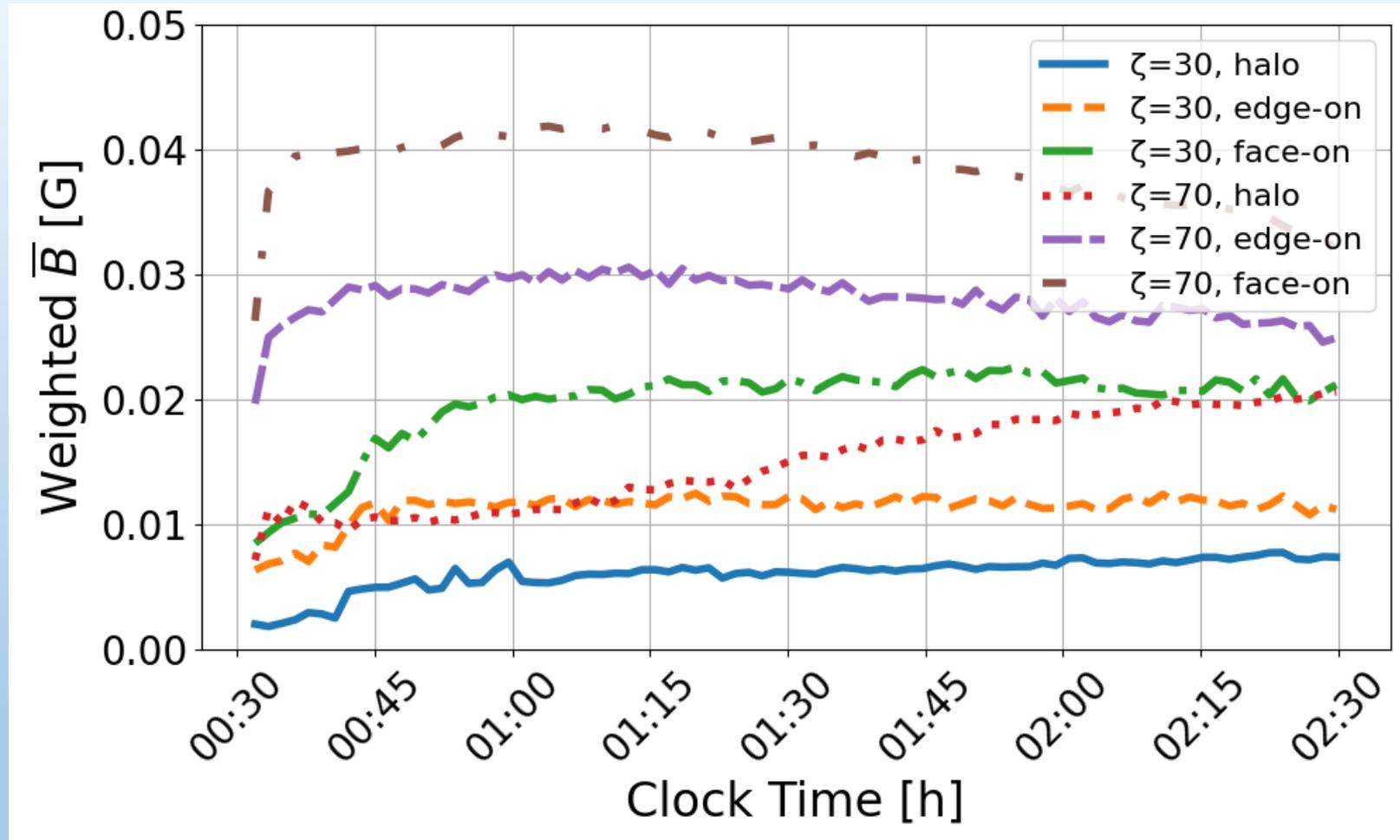
Husidic et al. (submitted)

# Intensity Curves

- Roll-over:
    - 165 – 300 MHz for  $\zeta = 30$
    - 65 – 145 MHz for  $\zeta = 70$
  - Lower roll-over frequencies observed at side/top views
  - Spectral shapes not yet power-law, but already steeper than analytical predictions
- $\alpha = (\delta - 1)/2$        $\alpha = 0.9\delta - 1.22$
- Strong self-absorption and evolving distributions steepen spectra early on
  - Idealised synchrotron/GS models miss key complexities in evolving CME environments
  - Observations often show steeper indices  $\rightarrow$  trend consistent with our particle transport simulations



# Weighted Magnetic Field Strength



# Itô Calculus

$$\frac{\partial f}{\partial t} + \frac{d\mathbf{x}}{dt} \cdot \nabla f + \frac{d\mu}{dt} \frac{\partial f}{\partial \mu} + \frac{dp}{dt} \frac{\partial f}{\partial p} = \frac{\partial}{\partial \mu} \left( D_{\mu\mu} \frac{\partial f}{\partial \mu} \right) + \nabla \cdot (\mathbf{D}_{\perp} \cdot \nabla f)$$

- The FTE is **equivalent** to the **stochastic differential equations (SDEs)**:

$$\begin{aligned} d\mathbf{x} &= \left( \frac{d\mathbf{x}}{dt} + \nabla \cdot \mathbf{D}_{\perp} \right) dt + \sqrt{2\mathbf{D}_{\perp}} d\mathbf{w}_{\mathbf{x}}, \\ d\mu &= \left( \frac{d\mu}{dt} + \frac{\partial D_{\mu\mu}}{\partial \mu} \right) dt + \sqrt{2D_{\mu\mu}} dw_{\mu}, \\ dp &= \frac{dp}{dt} dt, \end{aligned}$$

with  $\mathbf{w}_i$  being Wiener processes ( = Brownian motion )

- SDEs describe the trajectory of a **pseudo-particle** in phase space
- Pseudo-particle  $\approx$  phase space density element

# Itô Calculus

- **PARADISE** solves the FTE by integrating the equivalent SDEs forward in time, i.e.,

$$\begin{aligned}d\mathbf{x} &= \left( \frac{d\mathbf{x}}{dt} + \nabla \cdot \mathbf{D}_\perp \right) dt + \sqrt{2\mathbf{D}_\perp} d\mathbf{w}_\mathbf{x}, \\d\mu &= \left( \frac{d\mu}{dt} + \frac{\partial D_{\mu\mu}}{\partial \mu} \right) dt + \sqrt{2D_{\mu\mu}} dw_\mu, \\dp &= \frac{dp}{dt} dt,\end{aligned}$$



Integrate and  
sample  $\sim 10^8$   
pseudo-particles

- The average solar wind velocity and magnetic field are obtained from the 3D ideal MHD models **EUHFORIA** or **Icarus**
- The diffusion coefficient are derived from a composite slab/2D turbulence model with the assumptions of QLT or a non-linear theory (modular)

# Cross-Field Diffusion Coefficients

- Axis-symmetric cross-field diffusion tensor:  $\mathbf{D}_\perp = D_\perp (\mathbb{I} - \mathbf{b}\mathbf{b})$

- Perpendicular mean free path:  $\lambda_\perp = \frac{3}{v} \kappa_\perp = \frac{3}{2v} \int_{-1}^{+1} d\mu D_\perp(\mu)$

- Different assumptions about the turbulence give different diffusion coefficients

- Implemented in PARADISE (modular):

1. Non-linear guiding center theory

$$\lambda_\perp = \left[ 3^{(q+1)/2} D(s, q) \frac{\delta B_{2D}^2}{B_0^2} l_{2D}^{q+1} \right]^{2/(q+3)} \left[ \Gamma\left(\frac{1+q}{2}\right) \Gamma\left(\frac{1-q}{2}\right) \right]^{2/(q+3)} \lambda_\parallel^{(1-q)/(3+q)}$$

2. Field line random walk:  $\lambda_\perp = \sqrt{\frac{3(s-1)}{2(q-1)}} l_{2D} \frac{\delta B_{2D}}{B_0}$

3. Empirical models:

1. Dröge et al. (2010):  $\lambda_\perp = \alpha \lambda_\parallel r_g$      with  $r_g = \frac{\sqrt{1-\mu^2} p}{|q|B}$

2. Zhang et al. (2009):  $\lambda_\perp = \lambda_\perp^0 \left(\frac{p}{p_{\text{ref}}}\right)^{b_1} \left(\frac{B_{\text{ref}}}{B}\right)^{b_2}$

4.  $\lambda_\perp = \text{constant}$